Linear groups and group extensions are fundamental tools in many areas of algebra. Given a linear group extended by an infinite cyclic group, we construct a homomorphic image of the extension, dissect its structure, and discuss applications to asymptotic group theory.