

**The Jacobian Conjecture:** Let  $R = \mathbb{C}[x_1, \dots, x_n]$  be a polynomial ring in  $n$  variables over the complex numbers. If  $f_1, \dots, f_n \in R$ , then  $P(x_i) = f_i$  defines a  $\mathbb{C}$ -endomorphism of  $R$ . Associated with  $P$  is the  $n \times n$  matrix  $J(P) = (\partial f_i / \partial x_j)$  with entries in  $R$ . If  $P$  is an automorphism of  $R$ , then the chain rule implies that  $J(P)$  is an invertible matrix. The Jacobian Conjecture is that the converse holds: If  $J(P)$  is an invertible matrix, then  $P$  is a automorphism of  $R$ . The Jacobian Conjecture is true for  $n = 1$ , but is open for  $n \geq 2$ . For  $n \geq 3$ , there is little evidence for either the truth or falsity of the conjecture, but it is generally believed to be true for  $n = 2$ . I will discuss what is known when  $n = 2$ .