In the last few decades there has been an explosion of successful application of probability to solving some old open problems in discrete mathematics. In this talk we discuss a few very recent examples of such applications.