Square tilings are well known as a model for discretizing classical complex analysis. It seems reasonable that cube tilings would serve as a model for three-dimensions, and indeed they do -- up to a point. We will explore what does and does not work when we increase dimension and compare with the classical situation.